

Determine if the sequence is geometric. If it is, find the common ratio.

1. $-1, 6, -36, 216, \dots$

2. $-1, 1, 4, 8, \dots$

3. $4, 16, 36, 64, \dots$

4. $-3, -15, -75, -375, \dots$

5. $-2, -4, -8, -16, \dots$

6. $1, -5, 25, -125, \dots$

The following problems include given information from geometric sequences:

Find the first five terms and the 20th term

7. $a_n = 2 \cdot \left(\frac{1}{4}\right)^{n-1}$

8. $a_n = -4 \cdot 3^{n-1}$

Find the common ratio, the first five terms and the explicit formula

9. $\begin{aligned} a_n &= a_{n-1} \cdot 2 \\ a_1 &= 2 \end{aligned}$

10. $\begin{aligned} a_n &= a_{n-1} \cdot -3 \\ a_1 &= -3 \end{aligned}$

11. $\begin{aligned} a_n &= a_{n-1} \cdot 3 \\ a_1 &= -3 \end{aligned}$

Find the recursive formula and the next three terms in the sequence.

12. $a_1 = -4, r = 6$

13. $a_1 = 0.8, r = -5$

Find the 8th term, the recursive formula and the explicit formula.

14. $a_4 = -12$ and $a_5 = -6$

15. $a_5 = 768$ and $a_2 = 12$

16. $a_1 = -2$ and $a_5 = -512$

17. $a_5 = 3888$ and $a_3 = 108$

Evaluate each geometric series.

18. $\sum_{k=1}^7 4^{k-1}$

19. $\sum_{n=1}^8 2 \cdot (-2)^{n-1}$

20. $\sum_{n=1}^{10} 4 \cdot (-3)^{n-1}$

21. $2 - 10 + 50 - 250\dots, n = 8$

22. $-3 - 6 - 12 - 24\dots, n = 9$

23. $1 - 5 + 25 - 125\dots, n = 7$

24. $a_1 = 4, a_n = 1024, r = -2$

25. $a_1 = 4, a_n = 8748, r = 3$

Determine the number of terms n in each geometric series.

26. $a_1 = -2, r = 5, S_n = -62$

27. $a_1 = -3, r = 4, S_n = -4095$

28. $\sum_{m=1}^n -2 \cdot 4^{m-1} = -42$

29. $-4 + 16 - 64 + 256\dots, S_n = 52428$